# Temporal analysis of bibliographic networks 

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## ifffr Outline

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## Temporal networks

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A temporal network $\mathcal{N}_{T}=(\mathcal{V}, \mathcal{L}, \mathcal{P}, \mathcal{W}, \mathcal{T})$ is obtained by attaching the time, $\mathcal{T}$, to an ordinary network where $\mathcal{T}$ is a set of time points, $t \in \mathcal{T}$.
In a temporal network, nodes $v \in \mathcal{V}$ and links $I \in \mathcal{L}$ are not necessarily present or active in all time points. Let $T(v), T \in \mathcal{P}$, be the activity set of time points for node $v$ and $T(I), T \in \mathcal{W}$, the activity set of time points for link $I$.
Besides the presence/absence of nodes and links also their properties can change through time.

## Temporal quantities

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We introduce a notion of a temporal quantity

$$
a(t)= \begin{cases}a^{\prime}(t) & t \in T_{a} \\ \mathscr{H} & t \in \mathcal{T} \backslash T_{a}\end{cases}
$$

where $T_{a}$ is the activity time set of $a$ and $a^{\prime}(t)$ is the value of $a$ in an instant $t \in T_{a}$, and $\mathscr{H}$ denotes the value undefined.

We assume that the values of temporal quantities belong to a set $A$ which is a semiring $(A,+, \cdot, 0,1)$ for binary operations $+: A \times A \rightarrow A$ and $\cdot: A \times A \rightarrow A$.
We can extend both operations to the set $A_{\mathscr{H}}=A \cup\{\mathscr{H}\}$ by requiring that for all $a \in A_{\mathscr{H}}$ it holds

$$
a+\mathscr{H}=\mathscr{H}+a=a \quad \text { and } a \cdot \mathscr{H}=\mathscr{H} \cdot a=\mathscr{H} .
$$

The structure $\left(A_{\mathscr{H}},+, \cdot, \mathscr{H}, 1\right)$ is also a semiring.

## Semiring addition and multiplication in networks.

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In applications of semirings in analysis of graphs and networks the addition + describes the composition of values on parallel paths and the multiplication • describes the composition of values on sequential paths. For a combinatorial semiring these two schemes correspond to basic principles of combinatorics Rule of Sum and Rule of Product.

## ifff Operations with temporal quantities

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Let $A_{\mathscr{H}}(\mathcal{T})$ denote the set of all temporal quantities over $A_{\mathscr{H}}$ in time $\mathcal{T}$. To extend the operations to networks and their matrices we first define the sum (parallel links) $a+b$ as

$$
(a+b)(t)=a(t)+b(t) \quad \text { and } \quad T_{a+b}=T_{a} \cup T_{b} .
$$

The product (sequential links) $a \cdot b$ is defined as

$$
(a \cdot b)(t)=a(t) \cdot b(t) \quad \text { and } \quad T_{a \cdot b}=T_{a} \cap T_{b} .
$$

Let us define the temporal quantities $\mathbf{0}$ and $\mathbf{1}$ with requirements $\mathbf{0}(t)=\mathscr{H}$ and $\mathbf{1}(t)=1$ for all $t \in \mathcal{T}$. Again, the structure $\left(A_{\mathscr{H}}(\mathcal{T}),+, \cdot, \mathbf{0}, \mathbf{1}\right)$ is a semiring.

## $34 i$ <br> Semiring for temporal quantities

A semiring is also the set of square matrices of order $n$ over it for addition $\mathbf{A} \oplus \mathbf{B}=\mathbf{S}$

$$
s_{i j}=a_{i j}+b_{i j}
$$

and multiplication $\mathbf{A} \odot \mathbf{B}=\mathbf{P}$

$$
p_{i j}=\sum_{k=1}^{n} a_{i k} \cdot b_{k j}
$$

The matrix multiplication is closely related to traveling on networks. For a value $p_{i j}$ to be defined (different from $\mathscr{H}$ ) there should exist at least one node $k$ such that both link $(i, k)$ and link $(k, j)$ exist (at the same time) - the transition from the node $i$ to the node $j$ through a node $k$ is possible. Its contribution is $a_{i k} \cdot b_{k j}$.

## $i 4 f i$ <br> Temporal quantities on intervals

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In the following we shall limit our discussion to temporal quantities that can be described in the form of time-interval/value sequences

$$
a=\left(\left(I_{i}, v_{i}\right)\right)_{i=1}^{k}
$$

where $I_{i}$ is a time-interval, $T_{a}=\bigcup_{i=1}^{k} I_{i}$, and $v_{i}$ is a constant value of $a$ on this interval. To simplify the exposition we will assume in the following that all the intervals are of the form $\left[s_{i}, f_{i}\right), s_{i}$ is the starting time and $f_{i}$ is the finishing time. Therefore we can describe the temporal quantities with sequences

$$
a=\left(\left(s_{i}, f_{i}, v_{i}\right)\right)_{i=1}^{k}
$$

To provide a computational support for the proposed approach we are developing in Python a library TQ (Temporal Quantities). The following are two temporal quantities $a$ and $b$ represented in Python

```
a = [(1, 5, 2), (6, 8, 1), (11, 12, 3), (14, 16, 2),
    (17, 18, 5), (19, 20, 1)]
b = [(2, 3, 4), (4, 7, 3), (9, 10, 2), (13, 15, 5), (16, 21, 1)]
```

The temporal quantity a has on interval $[1,5)$ value 2 , on interval $[6,8)$ value 1 , on interval $[11,12$ ) value 3 , etc. Outside the specified intervals its value is undefined, $\mathscr{H}$.

## (iffif Sum and product of temporal quantities

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$$
\begin{aligned}
& \mathrm{a}=[(1,5,2),(6,8,1),(11,12,3),(14,16,2), \\
& \mathrm{b}=[(17,18,5),(19,20,1)], 4,4),(4,7,3),(9,10,2),(13,15,5),(16,21,1)]
\end{aligned}
$$

The following are the sum $s=a+b$ and the product $p=a \cdot b$ of temporal quantities $a$ and $b$ over combinatorial semiring.

$$
\begin{aligned}
s= & {[(1,2,2),(2,3,6),(3,4,2),(4,5,5),(5,6,3),} \\
& (6,7,4),(7,8,1),(9,10,2),(11,12,3), \\
& (13,14,5),(14,15,7),(15,16,2),(16,17,1), \\
& (17,18,6),(18,19,1),(19,20,2),(20,21,1)] \\
p= & {[(2,3,8),(4,5,6),(6,7,3),(14,15,10),} \\
& (17,18,5),(19,20,1)]
\end{aligned}
$$

They are visually displayed at the bottom half of figures on the following slides.

## Addition of temporal quantities.

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(iffif Multiplication of temporal quantities.

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In some applications over the combinatorial semiring we shall use the aggregated value of a temporal quantity $a=\left(\left(s_{i}, f_{i}, v_{i}\right)\right)_{i=1}^{k}$. It is defined as

$$
\Sigma a=\sum_{i=1}^{k}\left(f_{i}-s_{i}\right) \cdot v_{i}
$$

and is computed using the procedure total. For example $\Sigma a=23$ and $\Sigma b=30$. Note that $\Sigma a+\Sigma b=\Sigma(a+b)$.

## $i 4 f i$ <br> Networks from bibliographic data

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From special bibliographies (BibTEX) and bibliographic services (Web of Science, Scopus, SICRIS, CiteSeer, Zentralblatt MATH, Google Scholar, DBLP Bibliography, US patent office, and others) we can derive some two-mode networks on selected topics:

- works $\times$ authors (WA),
- works $\times$ keywords (WK);
and from some data also the network
- works $\times$ classification (WC), and the
- one-mode citation network works $\times$ works ( $\mathbf{C i}$ );
where works include papers, reports, books, patents etc.
Besides this we get also at least the partition of works by the journal or publisher and the partition of works by the publication year.

For converting WoS file into networks in Pajek's format a program WoS2Pajek was developed (in Python).

## Temporal co-occurrence networks

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Let the binary matrix $\mathbf{A}=\left[a_{e p}\right]$ describe a two-mode network on the set of events $E$ and the set of of participants $P$ :

$$
a_{e p}= \begin{cases}1 & p \text { participated in the event } e \\ 0 & \text { otherwise }\end{cases}
$$

The function $d: E \rightarrow \mathcal{T}$ assigns to each event $e$ the date $d(e)$ when it happened. $\mathcal{T}=[$ first, last $] \subset \mathbb{N}$. Using these data we can construct two temporal affiliation matrices:

- instantaneous $\mathbf{A i}=\left[a i_{e p}\right]$, where

$$
a i_{e p}= \begin{cases}{[(d(e), d(e)+1,1)]} & a_{e p}=1 \\ {[]} & \text { otherwise }\end{cases}
$$

- cumulative $\mathbf{A c}=\left[a c_{e p}\right]$, where

$$
a c_{e p}= \begin{cases}{[(d(e), \text { last }+1,1)]} & a_{e p}=1 \\ {[]} & \text { otherwise }\end{cases}
$$

## Multiplication of co-occurence networks

## Instantaneous

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Instantaneous $\mathbf{A}$ on $P \times A$ and $\mathbf{B}$ on $P \times B . \mathbf{C}=\mathbf{A}^{T} . \mathbf{B}$ on $A \times B$.

$$
c_{i j}(t)=\sum_{p \in P} a_{p i}(t)^{T} \cdot b_{p j}(t)
$$

$a_{p i}=\left[\left(d_{p i}, d_{p i}+1, v_{p i}\right)\right]$ and $b_{p j}=\left[\left(d_{p j}, d_{p j}+1, v_{p j}\right)\right]$
for $t=d$ we get

$$
c_{i j}=\left[\left(d, d+1, \sum_{p \in P: d_{p i}=d_{p j}=d} v_{p i} \cdot v_{p j}\right)\right]_{d \in \mathcal{T}}
$$

for $v_{p i}=v_{p j}=1$ we finally get

$$
v_{i j}(d)=\left|\left\{p \in P: d_{p i}=d_{p j}=d\right\}\right|
$$

For binary temporal two-mode networks $\mathbf{A}$ and $\mathbf{B}$ the value $v_{i j}(d)$ of the product $\mathbf{A}^{T}$. $\mathbf{B}$ is equal to the number of different members of $P$ with which both $i$ and $j$ have contact in the instant $d$.

## Multiplication of co-occurence networks

## Cumulative

Cumulative $\mathbf{A}$ on $P \times A$ and $\mathbf{B}$ on $P \times B . \mathbf{C}=\mathbf{A}^{T} . \mathbf{B}$ on $A \times B$.

$$
c_{i j}(t)=\sum_{p \in P} a_{p i}(t)^{T} \cdot b_{p j}(t)
$$

$a_{p i}=\left[\left(d_{p i}\right.\right.$, last $\left.\left.+1, v_{p i}\right)\right]$ and $b_{p j}=\left[\left(d_{p j}\right.\right.$, last $\left.\left.+1, v_{p j}\right)\right]$
for $t=d$ we get

$$
c_{i j}=\left[\left(d, d+1, \sum_{p \in P:\left(d_{p i} \leq d\right) \wedge\left(d_{p j} \leq d\right)} v_{p i} \cdot v_{p j}\right)\right]_{d \in \mathcal{T}}
$$

for $v_{p i}=v_{p j}=1$ we finally get

$$
v_{i j}(d)=\left|\left\{p \in P:\left(d_{p i} \leq d\right) \wedge\left(d_{p j} \leq d\right)\right\}\right|
$$

## $i 4 f i$ <br> Temporal co-authorship networks

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Using the multiplication of temporal matrices over the combinatorial semiring we get the corresponding instantaneous and cumulative co-occurrence matrices

$$
\mathbf{C i}=\mathbf{A i}^{T} \cdot \mathbf{A} \mathbf{i} \quad \text { and } \quad \mathbf{C} \mathbf{c}=\mathbf{A c}^{T} \cdot \mathbf{A c}
$$

A typical example of such a matrix is the papers authorship matrix WA where $E$ is the set of papers $W, P$ is the set of authors $A$ and $d$ is the publication year.
The triple $(s, f, v)$ in a temporal quantity $c i_{p q}$ tells that in the time interval $[s, f)$ there were $v$ events in which both $p$ and $q$ took part.
The triple ( $s, f, v$ ) in a temporal quantity $c c_{p q}$ tells that in the time interval $[s, f)$ there were in total $v$ accumulated events in which both $p$ and $q$ took part.

The diagonal matrix entries $c i_{p p}$ and $c c_{p p}$ contain the temporal quantities counting the number of events in the time intervals in which the participant $p$ took part.

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For an example, from a collection SN5 of network data about publications on social networks till 2008 we extracted data about 92 the most active researchers and transformed them to corresponding temporal networks: CiteInst, CiteCum, WAinst, WAcum, WKinst, WKcum and a partition W92 with outdegrees of works in the original WA network.
The matrices

$$
\mathbf{C o i}=\mathbf{W A} \mathbf{i}^{T} \cdot \mathbf{W A i} \quad \text { and } \quad \mathbf{C o c}=\mathbf{W A c}{ }^{T} \cdot \mathbf{W A c}
$$

describe the instantaneous co-autorship temporal network and the cumulative co-autorship temporal network.

## $i m f$

## 92 authors

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- ROBERTS_J

- valente_t
- latkin_c

- LITwin_H
- Yamaguch_K
- BERKMAN_L
- KIM_Y
- MARTIN_J
- SEIKKULA_J
- HIRSCH_B


SCHNEGG_M
SCHWEIZE_T

- COHEN_C
- HAMMER_M
- MLARDO_A
- scom
- leydesdo l
- MIKA_P
- Estrada_e
- PESCOSOL B
- LIN_N
- SMITH_R


## $34 i$ <br> Temporal co-authorship networks

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```
>>> import os, sys, datetime
>>> os.chdir("C:/Users/batagelj/work/Python/WoS/SN5/ten")
>>> from TQ import *
>>> wai = TQ.Ianus2Mat("WAinst.ten")
>>> wac = TQ.Ianus2Mat("WAcum.ten")
>>> list(wai.keys())
    ['dim', 'met', 'typ', 'nam', 'mat', 'til', 'tin', 'tit']
>>> wai['dim']
(1346, 92, 1970, 2008)
>>> WAi = wai['mat']; WAc = wac['mat']
>>> AWi = TQ.MatTrans(WAi); AWc = TQ.MatTrans(WAc)
>>> Coi = TQ.MatProd(AWi,WAi); Coc = TQ.MatProd(AWc,WAc)
>>> auNames = wai['nam'][nr:]
>>> ia=dict(zip(auNames,range(92)))
>>> Coi[ia['BORGATTI_S']][ia['EVERETT_M']]
[(1988, 1989, 1), (1989, 1990, 2), (1990, 1991, 4),
    (1991, 1992, 1), (1992, 1995, 2), (1996, 1998, 1),
    (1999, 2000, 3), (2003, 2004, 1), (2005, 2007, 1)]
>>> Coc[ia['BORGATTI_S']][ia['EVERETT_M']]
[(1988, 1989, 1), (1989, 1990, 3), (1990, 1991, 7),
    (1991, 1992, 8), (1992, 1993, 10), (1993, 1994, 12),
    (1994, 1996, 14), (1996, 1997, 15), (1997, 1999, 16),
    (1999, 2003, 19), (2003, 2005, 20), (2005, 2006, 21),
    (2006, 2008, 22)]
```


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Using the multiplication of temporal matrices over the combinatorial semiring on bibliographic matrices WA and WK we get the corresponding instantaneous and cumulative matrices

$$
\mathbf{A K i}=\mathbf{W} \mathbf{A i}^{T} \cdot \mathbf{W K i} \quad \text { and } \quad \mathbf{A K c}=\mathbf{W} \mathbf{A c}^{T} \cdot \mathbf{W K c}
$$

The triple $(s, f, v)$ in a temporal quantity $a k i_{a k}$ tells that in the time interval $[s, f$ ) the author a used the keyword $k v$ times (in $v$ works).
The triple $(s, f, v)$ in a temporal quantity $a k c_{a k}$ tells that in an instant $t$ in the time interval $[s, f)$ the author a used cumulatively (till time $t$ ) the keyword $k v$ times (in $v$ works).

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```
>>> wki = TQ.Ianus2Mat("WKinst.ten")
    >>> AKi = TQ.MatProd(AWi,wki['mat'])
>>> kwNames = wki['nam'][nr:]
>>> len(kwNames)
8571
>>> ik=dict(zip(kwNames,range(8571)))
>>> Bc = [ AKi[i][ik['centrality']] for i in range(92)]
>>> [auNames[i] for i in range(92) if Bc[i]!=[]]
['BORGATTI_S', 'CARLEY_K', 'GALASKIE_J', 'BURT_R', 'FREEMAN_L',
    'NEWMAN_M', 'BARABASI_A', 'WELLMAN_B', 'KNOKE_D', 'PAPPI_F',
    'HOLME_P', 'WATTS_D', 'JOHNSON_C', 'WHITE_D', 'BREWER_D',
    'MARSDEN_P', 'ROTHENBE_R', 'VALENTE_T', 'SNIJDERS_T',
    'KRACKHAR_D', 'WHITE_H', 'KILDUFF_M', 'LEYDESDO_L',
    'KLOVDAHL_A', 'MOODY_J', 'FRANK_O', 'BONACICH_P', 'BATAGELJ_V',
    'JOHNSON_J', 'FAUST_K', 'MIZRUCHI_M', 'YAMAGUCH_K',
    'FRIEDKIN_N', 'LAZEGA_E', 'CHEN_C', 'KILLWORT_P', 'ESTRADA_E',
    'BUTTS_C', 'EVERETT_M', 'FERLIGOJ_A', 'IACOBUCC_D']
```


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```
>>> T = [ (i,TQ.total(Bc[i])) for i in range(92) ]
>>> I = sorted(T,key=lambda e:e[1],reverse=True)
>>> [[auNames[i],v,Bc[i]] for (i,v) in I[:5]]
[['BORGATTI_S', 11, [(1991, 1992, 1), (1994, 1995, 1),
    (1997, 1998, 1), (1999, 2000, 2), (2003, 2004, 1),
    (2005, 2007, 2), (2007, 2008, 1)]],
    ['NEWMAN_M', 9, [(2001, 2002, 2), (2002, 2003, 1),
        (2004, 2005, 2), (2005, 2006, 1), (2006, 2007, 2),
        (2007, 2008, 1)]],
    ['BONACICH_P', 7, [(1986, 1988, 1), (1991, 1992, 1),
        (1998, 1999, 1), (2001, 2002, 1), (2004, 2005, 2)]],
    ['EVERETT_M', 6, [(1997, 1998, 1), (1999, 2000, 2),
        (2004, 2007, 1)]],
    ['CARLEY_K', 5, [(1999, 2000, 1), (2003, 2004, 1),
        (2006, 2007, 3)]]]
```


## Temporal citation networks

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A citation matrix $\mathbf{C i}$ describes the citation relation $p$ cites $q$. Note that $p$ cites $q \Rightarrow d(p) \geq d(q)$.
Then we can construct its instantaneus version Cii:

$$
c i i_{p q}=[(d(p), d(p)+1,1)] \quad \text { iff } \quad c i_{p q}=1
$$

and its cumulative version Cic:

$$
c i c_{p q}=[(d(p), \text { last }+1,1)] \quad \text { iff } \quad c i_{p q}=1
$$

Temporal versions of:
Bibliographic coupling biCo $=\mathbf{C i} \cdot \mathbf{C i}^{T}$.
Co-citation $\mathbf{c o C i}=\mathbf{C i}{ }^{T}$. $\mathbf{C i}$.
Citations between authors $\mathbf{C a}=\mathbf{W A}^{T} . \mathbf{C i} \cdot \mathbf{W A}$.

$$
\mathbf{A C A}=\mathbf{W A i}{ }^{T} \cdot \mathbf{C i i} \cdot \mathbf{W A c}
$$

## iffic Citations between authors

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```
>>> cite = TQ.Ianus2Mat("CiteInst.ten")
>>> Cite = cite['mat']; WAc = wac['mat']
>>> ACA = TQ.MatProd(TQ.MatProd(AWi,Cite),WAc)
>>> ACA[ia['WASSERMA_S']][ia['HOLLAND_P']]
[(1977, 1978, 1), (1980, 1981, 5), (1981, 1982, 2),
    (1984, 1985, 2), (1985, 1986, 1), (1987, 1989, 2),
    (1990, 1991, 1), (1991, 1992, 2), (1992, 1994, 3),
    (1995, 1996, 2), (1996, 1997, 3), (1999, 2000, 5),
    (2000, 2001, 1), (2006, 2008, 1)]
>>> D = [(i,TQ.total(ACA[ia['DOREIAN_P']][i])) for i in range(92)
>>> J = sorted(D,key=lambda e:e[1],reverse=True)
>>> [[auNames[i],v,ACA[ia['DOREIAN_P']][i]] for (i,v) in J[:5]]
[['DOREIAN_P', 69, [(1980, 1983, 1), (1984, 1985, 2),
        (1985, 1986, 1), (1986, 1987, 3), (1987, 1988, 2),
        (1988, 1989, 7), (1989, 1990, 5), (1990, 1991, 2),
        (1992, 1993, 6), (1994, 1995, 8), (1995, 1996, 2),
        (1996, 1997, 4), (2000, 2001, 3), (2001, 2004, 4),
        (2004, 2005, 6), (2006, 2007, 3)]],
    ['BREIGER_R', 26, [(1980, 1981, 3), (1984, 1986, 1),
        (1986, 1987, 2), (1987, 1988, 1), (1988, 1989, 4),
        (1989, 1990, 1), (1992, 1993, 3), (1994, 1995, 2),
        (1995, 1996, 1), (1996, 1997, 2), (2000, 2001, 1),
        (2004, 2005, 2), (2007, 2008, 2)]]
```


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['BURT_R', 20, [(1985, 1986, 3), (1986, 1987, 1), (1987, 1988, 2), (1988, 1989, 5), (1989, 1990, 2), (1992, 1993, 4), $(1994,1995,1),(2000,2001,1)$, (2004, 2005, 1)]],
['BATAGELJ_V', 17, [(1992, 1993, 2), (1994, 1995, 2), (1996, 1997, 4), ( $2000,2001,4),(2004,2005,5)]]$,
['FARARO_T' $15,[(1984,1985,1),(1985,1986,2)$, (1988, 1989, 2), (1989, 1990, 1), (1992, 1993, 1), (1995, 1996, 1), (2001, 2002, 3), (2002, 2003, 2), ( $2003,2004,1),(2006,2007,1)]$ ]
>>>

## Conclusions

- temporal networks approach can give additional insight into bibliographic networks;
- we presented only some examples to show that it works. Many options have still to be elaborated;
- temporal networks methods produce large results. Special methods for identifying and presenting (visualizing) interesting parts need to be developed;
- current version of TQ library is based on matrices. This limits the application of the proposed methods to some thousands of nodes (space and time complexity). The limits can be partially extended by switching to graph representation.

